## Strategies for Spatial Joins

- Recall Spatial Join Example:
- List all pairs of overlapping rivers and countries.
- Return pairs from "rivers" table and "countries" table satisfying the "overlap" predicate.



## Strategies for Spatial Joins - Continued

- List of strategies
- Nested loop:
- Test all possible pairs for spatial predicate
- All rivers are paired with all countries
- Space Partitioning:
- Test pairs of objects from common spatial regions only
- Rivers in Africa are tested with countries in Africa only
- Tree Matching
- Hierarchical pairing of object groups from each table
- Other, e.g. spatial-join-index based, external plane-sweep, ...


## Spatial Join - Running Examples



Overlay \& spatial join


Results:

Query:
For each fire station, find all the houses within a distance <= 1

| Fire-stations | Houses |
| :---: | :---: |
| A | a |
| B | f |
| D | h |
| D | j |

Nested loop


## Query:

For each fire station, find all the houses within a distance <= 1

Suppose: 1) each data block has 2 points
2) the size of memory buffer is 3 blocks (i.e., 1 for fire-stations, 1 for houses, 1 for results)

## Algorithm:

## For each block $B_{f s}$ of fire stations

For each block $B_{h}$ of houses
Scan all pairs of fire stats in $B_{f s}$ and houses in $B_{h}$

## Nested loop



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For each fire station, find all the houses within a distance <= 1

Suppose: 1) each data block has 2 points
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## Algorithm:

## For each block $\mathrm{B}_{\mathrm{fs}}$ of fire stations

## For each block $B_{h}$ of houses

Scan all pairs of fire stats in $B_{f s}$ and houses in $B_{h}$
For Block 0, traverse through Blocks 2-7
For Block 1, traverse through Blocks 2-7

## cost:

\# blocks for fire stations * \# blocks for houses $=2 * 6=12$


## Nested loop with Index for Inner Loop



Query:
For each fire station, find all the houses within a distance <= 1

Suppose an R-tree (primary index) is available for the houses.


Nested loop with Index for Inner Loop


Query:
For each fire station, find all the houses within a distance <= 1

For each block of fire stations, create MOBR with length of 1.

Nested loop with Index for Inner Loop


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For each block of fire stations, create MBR with length of 1.

## Algorithm:

For each MBR $\mathrm{M}_{\mathrm{fs}}$ of fire-station blocks
Find overlapped blocks in the R-tree

Nested loop with Index for Inner Loop


Query:
For each fire station, find all the houses within a distance <= 1

## Algorithm:

For each MBR $\mathrm{M}_{\mathrm{fs}}$ of fire-station blocks Find overlapped blocks in the R-tree


Block 0:

$$
\begin{aligned}
& \text { Root -> X -> },->\text { leaf objs } \\
& ->Y \text {-> }->\text { leaf objs }
\end{aligned}
$$



Nested loop with Index for Inner Loop


Query:
For each fire station, find all the houses within a distance <= 1

Algorithm:
For each MBR $\mathrm{M}_{\mathrm{fs}}$ of fire-station blocks Find overlapped blocks in the R-tree


Block 1:

$$
\begin{aligned}
\text { Root }->X \text {-> } & \text {-> leaf objs } \\
\quad>Y \text {-> } & \text {-> leaf objs }
\end{aligned}
$$



## Tree Matching strategy



Query:
For each fire station, find all the houses within a distance <= 1

Suppose an R-tree (primary index) is available for fire stations and houses, respectively.


## Tree Matching strategy




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For each fire station, find all the houses within a distance <= 1

Suppose an R-tree (primary index) is available for fire stations and houses, respectively.

Algorithm:
Tree Match(Rtree1 node1, Rtree2 node2)
For all MBR M2 of R-tree2 node2
For all MBR M1 of R-tree1 node1
IF (if mindist(M2,M1) $=<1$ )
If (node1 and node2 are leaves) <perform the join>
Else if (node1 is leaf page)
Read child of M2
Tree Match (node1, M2.child)
Else if(node2 is a leaf page)

## Tree Matching strategy



Query:
For each fire station, find all the houses within a distance <= 1

Suppose an R-tree (primary index) is available for fire stations and houses, respectively.


## Partitioning based strategy



Partition the study area into 2 * $2=4$ partitions, $\mathrm{P}_{0}, \mathrm{P}_{1}, \mathrm{P}_{2}, \mathrm{P}_{3}$

For fire station, create MBR with length of 1.

Partitioning results:

| Partition | Fire-Stations | Houses |
| :---: | :---: | :---: |
| $P_{0}$ | $A$ | $a, b, c, e$ |
| $P_{1}$ | $B, C$ | $d, f$ |
| $P_{2}$ | $D$ | $\mathrm{~g}, \mathrm{~h}, \mathrm{j}$ |
| $\mathrm{P}_{3}$ | C | $\mathrm{i}, \mathrm{k}, \mathrm{l}$ |

MBR of $C$ in both $P_{1}$ and $P_{3}$ since it overlaps both partitions.

## Partitioning based strategy



Query:
For each fire station, find all the houses within a distance <= 1

## Algorithm:

For each partition $\mathrm{P}_{\mathrm{i}}$
For each MOBR $\mathrm{M}_{\mathrm{fs}}$ of fire-station in $\mathrm{P}_{\mathrm{i}}$
Find all the houses in $P_{i}$ that are overlapped with $\mathrm{M}_{\mathrm{fs}}$

Results from filter phase:

| Partition | MOBR | Houses overlapped |
| :---: | :---: | :---: |
| $P_{0}$ | $A$ | $a, b, c, e$ |
| $P_{1}$ | $B$ | $f$ |
| $P_{2}$ | $D$ | $d, f$ |
| $P_{3}$ | $C$ | $h, j$ |

## Strategies for 1-Nearest Neighbor Queries

- Recall Nearest Neighbor Example
- Find the city closest to Chicago.
- Return one spatial object from datafile C

- List of strategies
- Two phase approach
- Fetch C's disk sector(s) containing the location Chicago
- $M=$ minimum distance(Chicago, cities in fetched sectors)
- Test all cities within distance M of Chicago (Range Query)
- Single phase approach
- Recursive algorithm for R-tree
- First get the closest data point
- Then eliminate objects based on mindist to MBRs
- Similar to K-NN algorithm on KD-trees


## Two Phase Approach



Given the location of a user p, find the nearest restaurant.
(If more than one nearest neighbors, return all results)

Suppose R-tree (primary index) is available on this dataset


## Two Phase Approach

Given the location of a user p, find the nearest restaurant.
(If more than one nearest neighbors, return all results)

## Algorithm:

Find the index leaf containing the query point $p$
Point g, $h$ are the closest points to $p$,


## Two Phase Approach

Given the location of a user $p$, find the nearest restaurant.
(If more than one nearest neighbors, return all results)

## Algorithm:

Find the index leaf containing the query point $p$
Point $g$, $h$ are the closest points to $p$ at distance $d_{B}$ Create a circle Circle ${ }_{p}$ whose center is $p$, and radius $=d_{B}$ Create the MOBR of Circle $_{p}: M_{p}$
Range query: $\mathrm{M}_{\mathrm{p}}$, and test all points in $\mathrm{M}_{\mathrm{p}}$ Root -> Y -> leaves containing <g,h> and <j,i> Since $\operatorname{dist}(p, j)=1.41<D_{B}$, point $j$ is nearest neighbor of $p$


## One Phase Approach - Recursive search on R-tree

Given the location of a user p, find the nearest restaurant.
(If more than one nearest neighbors, return all results)

| Algorithm: | Node | MinDist | MaxDist |  |
| :---: | :---: | :---: | :---: | :---: |
| First level: | X | 3 | 7.47 | Nothing X eliminated |
|  | Y | 0 | 4.47 | Nothing eliminated |
| Second level: |  | 3.16 | 4.12 |  |
|  |  | 3.16 | 5.10 | Node eliminated |
|  |  | 4.47 |  |  |
|  |  | 0 | 2.83 |  |
|  |  | 1.41 | 2.83 |  |
|  |  | 3.16 |  | Node eliminated |

In the first part of the algorithm we get that Point g, h are the closest points to p , distance $=2$

